

Figure 11. Phase diagram for the ternary mixture of nitrogen, carbon dioxide, and *n*-butane, at  $T = 310.9$  K and  $P = 206.8$  bar (3000 psia) fit with the Peng–Robinson equation of state.

### Conclusions

A new, high-pressure vapor–liquid equilibrium apparatus capable of measuring the compositions and densities of the coexisting phases up to 300 °F and 5000 psia has been built, tested, and used to obtain data for the  $\text{CO}_2 + n$ -butane,  $\text{N}_2 +$

*n*-butane, and  $\text{N}_2 + \text{CO}_2 + n$ -butane systems. Data for the first of these systems are in excellent agreement with previously published data for both compositions and densities. The compositional data for the  $\text{CO}_2 + n$ -butane system were fit well with the Peng–Robinson equation of state with van der Waals one-fluid mixing rules, though (as is expected) the liquid density predictions were poor. Both the compositions and densities of the  $\text{N}_2 + n$ -butane system are poorly fit in this way, as is typical of  $\text{N}_2$ –hydrocarbon systems. Since the constituent binary systems were poorly fit with the Peng–Robinson equation of state, so was the data for the ternary  $\text{N}_2 + \text{CO}_2 + n$ -butane system.

Registry No.  $\text{N}_2$ , 7727-37-9;  $\text{CO}_2$ , 124-38-9; butane, 106-97-8.

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## Vapor–Liquid Equilibria at 760 mmHg in the Ternary System Methyl Acetate–Propyl Bromide–Toluene

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Vapor–liquid equilibria at atmospheric pressure have been determined for the title ternary system. The data were correlated by various equations, and the appropriate parameters are reported.

The present work was undertaken to measure VLE data for the ternary system methyl acetate–propyl bromide–toluene for which no isobaric data are available. Data for the pertinent binaries have been reported previously (1, 2).

### Experimental Section

**Purity of Materials.** Methyl acetate (99.2+%) and propyl bromide (99.4+%) were purchased from Merck, and toluene (99.6+%) was purchased from Frutarom. The reagents were used without further purification after gas chromatography failed to show any significant impurities. Properties of the pure

Table I. Physical Constants of Pure Components

index	compd	refract. index at 25 °C	bp(760 mmHg), °C	purity GLC (min)
1	methyl acetate	1.3588 <sup>a</sup>	56.94 <sup>a</sup>	99.2
		1.3589 <sup>b</sup>	56.94 <sup>b</sup>	
2	propyl bromide	1.4320 <sup>a</sup>	70.55 <sup>a</sup>	99.4
		1.4317 <sup>b</sup>	70.80 <sup>b</sup>	
3	toluene	1.4926 <sup>a</sup>	110.70 <sup>a</sup>	99.6
		1.4941 <sup>b</sup>	110.63 <sup>b</sup>	

<sup>a</sup> Measured. <sup>b</sup> Reference 10.

components appear in Table I.

**Apparatus and Procedure.** An all-glass modified Dvorak and Boublik recirculation still (3) was used in the equilibrium determination. The experimental features have been described in previous publications (4). All analyses were carried out by gas chromatography on a Packard-Becker Model 417 apparatus provided with a thermal conductivity detector and an Autolab Model 6300 electronic integrator. The column was 200 cm long and 0.2 cm in diameter, was packed with OV-17 20%, and

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Table II. Experimental Vapor-Liquid Equilibria Data for Methyl Acetate (1)-Propyl Bromide (2)-Toluene (3) at 760 mmHg

$t, ^\circ\text{C}$	$x_1$	$x_2$	$x_3$	$y_1$	$y_2$	$y_3$	$\gamma_1$	$\gamma_2$	$\gamma_3$
58.51	0.885	0.062	0.053	0.942	0.051	0.007	1.0099	1.2319	0.6810
59.14	0.856	0.079	0.070	0.930	0.067	0.003	1.0104	1.2480	0.2130
59.72	0.658	0.274	0.068	0.776	0.223	0.001	1.0761	1.1600	0.0774
61.59	0.625	0.209	0.166	0.786	0.188	0.026	1.0797	1.2053	0.7589
61.93	0.378	0.596	0.026	0.510	0.480	0.010	1.1454	1.0695	1.8389
62.08	0.626	0.187	0.186	0.803	0.162	0.035	1.0830	1.1451	0.8989
63.01	0.472	0.369	0.160	0.655	0.316	0.029	1.1400	1.0973	0.8406
63.31	0.306	0.659	0.035	0.440	0.550	0.010	1.1688	1.0593	1.3147
63.31	0.404	0.473	0.123	0.572	0.409	0.020	1.1489	1.0980	0.7304
63.71	0.636	0.104	0.260	0.842	0.095	0.062	1.0623	1.1475	1.0867
63.80	0.355	0.515	0.130	0.532	0.447	0.021	1.1983	1.0848	0.7441
63.99	0.600	0.112	0.289	0.842	0.097	0.061	1.1159	1.0840	0.9392
64.10	0.587	0.114	0.299	0.841	0.097	0.062	1.1358	1.0566	0.9180
64.80	0.283	0.616	0.101	0.439	0.542	0.019	1.2036	1.0656	0.8173
64.95	0.502	0.212	0.286	0.742	0.193	0.065	1.1404	1.0970	0.9808
65.01	0.554	0.129	0.317	0.812	0.115	0.073	1.1292	0.0721	0.9888
65.04	0.446	0.206	0.349	0.748	0.184	0.068	1.2918	1.0748	0.8354
65.26	0.193	0.793	0.014	0.310	0.688	0.002	1.2248	1.0358	0.6179
65.41	0.477	0.234	0.289	0.715	0.216	0.068	1.1395	1.0970	1.0070
65.6	0.309	0.513	0.178	0.489	0.470	0.041	1.1974	1.0802	0.9627
65.66	0.230	0.686	0.085	0.372	0.612	0.016	1.2200	1.0527	0.7945
66.45	0.406	0.295	0.299	0.649	0.275	0.076	1.1767	1.0717	1.0360
66.53	0.572	0.038	0.391	0.868	0.026	0.106	1.1150	0.7886	1.1036
66.92	0.295	0.481	0.224	0.494	0.452	0.054	1.2158	1.0655	0.9652
67.12	0.158	0.785	0.058	0.272	0.717	0.012	1.2434	1.0282	0.8138
67.36	0.224	0.591	0.185	0.395	0.558	0.047	1.2560	1.0567	1.0010
67.62	0.160	0.748	0.092	0.279	0.701	0.020	1.2396	1.0386	0.8611
67.65	0.332	0.377	0.291	0.559	0.363	0.078	1.1939	1.0677	1.0480
67.75	0.193	0.661	0.146	0.333	0.629	0.038	1.2187	1.0511	1.0135
67.93	0.399	0.254	0.347	0.670	0.238	0.092	1.18032	1.0309	1.0216
68.16	0.225	0.580	0.195	0.400	0.553	0.048	1.2391	1.0386	0.9407
68.30	0.131	0.785	0.084	0.238	0.742	0.020	1.2632	1.0264	0.9187
68.45	0.141	0.758	0.101	0.256	0.720	0.024	1.2560	1.0272	0.8876
68.85	0.278	0.424	0.298	0.494	0.425	0.082	1.2128	1.0685	1.0272
69.13	0.109	0.821	0.070	0.199	0.783	0.018	1.2330	1.0102	0.9715
69.30	0.401	0.170	0.429	0.715	0.164	0.121	1.2026	1.0167	1.0385
69.37	0.085	0.864	0.051	0.151	0.836	0.013	1.1909	1.0170	0.9360
69.95	0.302	0.324	0.374	0.571	0.327	0.102	1.2489	1.0413	0.9791
70.05	0.317	0.289	0.394	0.596	0.290	0.114	1.2394	1.0343	1.0317
70.34	0.321	0.280	0.399	0.608	0.279	0.112	1.2381	1.0170	0.9975
71.25	0.367	0.141	0.492	0.710	0.144	0.146	1.2294	1.0175	1.0177
71.46	0.218	0.426	0.357	0.428	0.457	0.115	1.2414	1.0588	1.0971
71.72	0.267	0.313	0.420	0.528	0.339	0.133	1.2418	1.0601	1.0636
71.94	0.157	0.563	0.281	0.312	0.599	0.089	1.2421	1.0335	1.0630
72.08	0.144	0.592	0.264	0.290	0.627	0.083	1.2465	1.0250	1.0482
72.71	0.382	0.064	0.554	0.755	0.068	0.018	1.2040	1.0116	1.0372
74.36	0.051	0.757	0.192	0.095	0.840	0.065	1.0776	1.0045	1.0383
75.84	0.347	0.030	0.623	0.735	0.020	0.245	1.1763	0.5809	1.1470
76.41	0.176	0.343	0.481	0.413	0.416	0.172	1.2803	1.0317	1.0211
76.47	0.182	0.328	0.489	0.429	0.398	0.173	1.2840	1.0294	1.0101
76.71	0.223	0.215	0.562	0.525	0.256	0.219	1.2766	1.0043	1.1014
77.01	0.170	0.344	0.486	0.405	0.423	0.173	1.2780	1.0274	0.9975
78.31	0.075	0.552	0.373	0.159	0.690	0.151	1.1031	1.0074	1.0859
79.11	0.107	0.437	0.456	0.260	0.561	0.179	1.2304	1.0118	1.0210
79.80	0.252	0.060	0.688	0.647	0.063	0.289	1.2775	0.8135	1.0705
79.95	0.230	0.102	0.669	0.605	0.124	0.271	1.3013	0.9382	1.0278
80.52	0.143	0.295	0.562	0.358	0.397	0.246	1.2195	1.0167	1.0874
81.80	0.133	0.284	0.582	0.342	0.395	0.263	1.2038	1.0135	1.0776
82.60	0.148	0.219	0.633	0.399	0.313	0.288	1.2368	1.0203	1.0556
82.85	0.163	0.205	0.632	0.428	0.283	0.289	1.2006	0.9788	1.0519
84.34	0.094	0.312	0.594	0.247	0.460	0.293	1.1489	1.0040	1.0797
84.65	0.211	0.122	0.666	0.510	0.154	0.337	1.0475	0.8479	1.0963
84.93	0.164	0.127	0.709	0.450	0.187	0.363	1.1821	0.9843	1.1013
85.10	0.168	0.113	0.719	0.480	0.151	0.369	1.2245	0.8949	1.0966
87.39	0.101	0.218	0.681	0.284	0.342	0.374	1.1355	0.9818	1.0900
92.55	0.107	0.043	0.850	0.408	0.083	0.509	2.0283	1.0292	1.0318
94.13	0.084	0.067	0.849	0.325	0.130	0.545	1.2411	0.9996	1.0510
94.46	0.074	0.150	0.776	0.229	0.262	0.509	0.9783	0.8839	1.0634
95.60	0.048	0.109	0.844	0.210	0.226	0.565	1.3509	1.0186	1.0470
103.84	0.032	0.022	0.946	0.133	0.047	0.801	1.1865	0.8265	1.0306
103.90	0.029	0.020	0.951	0.149	0.047	0.804	1.2568	0.9480	1.0273

operated at 95 °C. Injector and detector temperatures were 210 and 220 °C, respectively. Very good separation was achieved under these conditions, and calibration analyses were carried out to convert the peak ratio to the weight composition

of the sample. Concentration measurements were accurate to better than  $\pm 1\%$ . The accuracy in determination of pressure and temperature was  $\Delta P = \pm 1$  mmHg and  $\Delta t = \pm 0.02$  °C.

**Table III. Vapor-Pressure Constants (10)**

compound	$\alpha_i$	$\beta_i$	$\delta_i$
methyl acetate	7.06131	1156.43	219.69
propyl bromide	6.91065	1194.889	225.51
toluene	6.95464	1344.800	219.482

**Results**

The temperature-concentration measurements at 760 mmHg for the ternary system are reported in Table II as well as the activity coefficients which were calculated from the following equation (5):

$$\ln \gamma_i = \ln (yP/xP_i^\circ) + (B_{ii} - V_i^L)(P - P_i^\circ)/RT + (P/RT) \sum_{j=1}^n \sum_{k=1}^n y_j y_k (\delta_{ij} - \delta_{jk}) \quad (1)$$

where

$$\delta_{ij} = 2B_{ij} - B_{jj} - B_{ii} \quad (2)$$

Vapor pressure  $P_i^\circ$  was calculated according to the Antoine equation:

$$\log P_i^\circ = \alpha_i - \beta_i/(\delta_i + t) \quad (3)$$

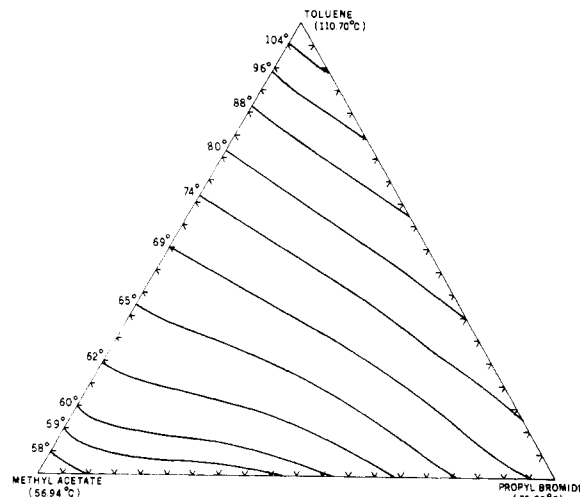
where the constants are reported in Table III. The molar virial coefficients  $B_{ij}$  and the mixed molar coefficient  $B_{ij}$  were calculated by the method of Tsonopoulos (6) using the molecular parameters suggested by the same author.

The ternary data reported in Table II were found to be thermodynamically consistent by the McDermott-Ellis method (7), modified by Wisniak and Tamir (8).

The activity coefficients were correlated by the following equation reported by Redlich and Kister (5):

$$\ln \gamma_1 = x_2 x_3 [B_{12} + B_{13} - B_{23}] + C_{12}(2x_1 - x_2) + C_{13}(2x_1 - x_3) + 2C_{23}(x_3 - x_2) + D_{12}(x_1 - x_2)(3x_1 - x_2) + D_{13}(x_1 - x_3)(3x_1 - x_2) - 3D_{23}(x_3 - x_2)^2 + C_1(1 - 2x_1)] + x_2^2 [B_{12} + C_{12}(3x_1 - x_2) + D_{12}(x_1 - x_2)(5x_1 - x_2)] + x_3^2 [B_{13} + C_{13}(3x_1 - x_3) + D_{13}(x_1 - x_3)(5x_1 - x_3)] \quad (4)$$

$B_{ij}$ ,  $C_{ij}$ , and  $D_{ij}$  are the binary constants and  $C_1$  is a ternary constant in Table IV. The equations for two other activity coefficients were obtained by cyclic rotation of the indices. The

**Figure 1. Isothermals for the ternary system (760 mmHg).**

binary data used for calculating the binary constants were reported elsewhere (1, 2).

The binary and ternary Redlich-Kister coefficients were obtained by the Simplex optimization algorithm and are reported in Table IV. Comparison of the relative values of the root mean square deviation for the cases with and without ternary constant  $C_1$  suggest that the predictor with a ternary constant is only slightly better.

The boiling temperature of the mixture was correlated solely with the liquid composition by the following equation, which has been derived on the basis of the concept of "excess property" (9):

$$T = \sum_{i=1}^n x_i T_i^\circ + \sum_{i=1}^{n-1} \sum_{j=i+1}^n x_i x_j [A_{ij} + B_{ij}(x_i - x_j) + C_{ij}(x_i - x_j)^2 \dots] \quad (5)$$

This equation is useful for obtaining isothermals and for exploring the azeotropic behavior and distillation paths of ternary mixtures (9). The coefficients  $A_{ij}$ ,  $B_{ij}$ , and  $C_{ij}$  are multicomponent parameters which are determined directly from the multicomponent data. Figure 1 reports the isothermals obtained on the basis of the parameters  $A_{ij}$  and  $B_{ij}$  reported in Table V by applying eq 5 for  $n = 3$ .

**Table IV. Redlich-Kister Correlation of Binary and Ternary Data**

system	$B_{ij}$	$C_{ij}$	$D_{ij}$	rmsd		
				$\gamma_1$	$\gamma_2$	$\gamma_3$
methyl acetate (1)-propyl bromide (2)	0.57896	0.00655	0.000164	0.193	0.0830	
methyl acetate (1)-toluene (3)	0.39979	-0.05466	0.12619	0.0172		0.0349
propyl bromide (2)-toluene (3)	-0.02429	$0.9014 \times 10^{-4}$	$0.8092 \times 10^{-6}$		0.0788	0.0643
				overall rmsd <sup>a</sup>		
system	$C_1$			$\gamma$		$y$
methyl acetate (1)-propyl bromide (2)-toluene (3)	0 -1.9399			0.209 0.170		0.033 0.023

<sup>a</sup>Lumped ternary data.

**Table V. Parameters of  $T$ - $x$  Correlation (Eq 5,  $n = 3$ ) for Methyl Acetate (1)-Propyl Bromide (2)-Toluene (3) at 760 mmHg<sup>a</sup>**

$ij$	$A_{ij}$	$B_{ij}$	$C_{ij}$	$D_{ij}$	$E_{ij}$	$F_{ij}$	$G_{ij}$	mean $D\%$	rmsd
12	-19.341	5.4133	-1.583					0.148	0.0298
13	-53.956	32.975	-32.688	16.095	33.602	25.318	-65.404	1.79	0.196
23	-20.759	5.5655	12.836	-6.485				0.213	0.0507
Ternary Parameters									
12	-17.833	9.0536	12.453					0.440	0.0694
13	-59.527	34.028	-6.9215						
23	-21.279	3.9775	5.7545						

<sup>a</sup> $T_1^\circ = 330.09$  K;  $T_2^\circ = 383.85$  K;  $T_3^\circ = 343.70$  K.  $D = |(T_{\text{obsd}} - T_{\text{calcd}})|/T_{\text{obsd}}$ . Mean  $D\% = (100/n)\sum D_i$ .

None of the three possible binaries exhibit azeotropic behavior, and as shown by Figure 1, neither does the ternary system. Table V contains also the group of parameters  $A_{ij}$ ,  $B_{ij}$ , and  $C_{ij}$  for the  $T-x$  correlation (eq 5) which yield the smaller mean deviation between the calculated and observed values of  $T$ .

#### Acknowledgment

Yehudit Reizner and Moshe Golden helped in the experimental work and numerical calculations.

#### Glossary

$A_{ij}$ , $B_{ij}$ , etc.	multicomponent adjustable parameters in eq 5
$B_{ij}$ , $B_{ij}$	virial coefficients, eq 2
$B_{ij}$ , $C_{ij}$ , $D_{ij}$	Redlich-Kister constants, eq 4
$V_i^L$	molar volume, component $i$
$n$	number of components
$P$	total pressure, mmHg
$P_i^\circ$	vapor pressure of pure component $i$ , mmHg
$T$	boiling temperature of a mixture, K
$T_i^\circ$	boiling temperature of pure component $i$ , K
$t$	temperature, °C

$x_i$ , $y_i$	mole fraction of component $i$ in the liquid and vapor phases
$\alpha_i$	coefficient, Antoine equation
$\beta_i$	coefficient, Antoine equation
$\gamma_i$	activity coefficient of component $i$
$\delta_i$	coefficient, Antoine equation
$\delta_{ij}$	virial coefficient parameter, eq 2

#### Subscripts

calcd	calculated
obsd	observed

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## The Systems Vinyl Acetate-Toluene and Vinyl Acetate-Propyl Bromide-Toluene

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Vapor-liquid equilibrium at 760 mmHg has been determined for the title systems. The binary vinyl acetate-toluene deviates positively from ideal behavior and does not have an azeotrope. The binary and ternary data were correlated by various equations, and the appropriate parameters are reported.

The present work was undertaken to measure VLE data for the title systems for which no isobaric data are available. Data for the two other binaries have already been measured (1, 2).

#### Experimental Section

**Purity of Materials.** Vinyl acetate analytical grade (99%+) was purchased from Fluka, propyl bromide (99.4%) from Merck, and analytical grade toluene (99.6%+) from Frutarom. The reagents were used without further purification after gas chromatography failed to show any significant impurities. Properties of the pure components appear in Table I.

**Apparatus and Procedure.** An all-glass modified Dvorak and Boublik recirculation still (3) was used in the equilibrium determination. A vacuum system connected the vapor condenser with a Swietoslowski ebullimeter and allowed total pressure regulation. The total pressure of the system was determined from the boiling temperature of the distilled water in the ebullimeter. The experimental features have been described in a previous publication (4). All analyses were carried out by gas chromatography on a Packard-Becker Model 417 apparatus provided with a thermal conductivity detector and a Spectra

Table I. Physical Constants of Pure Components

index	compd	refractive index (25 °C)	bp (760 mmHg), °C	purity, GLC (min)
1	vinyl acetate	1.3932 <sup>a</sup> 1.3934 <sup>c</sup>	72.56 <sup>a</sup> 72.49 <sup>c</sup>	99
2	propyl bromide	1.4320 <sup>a</sup> 1.4317 <sup>b</sup>	70.55 <sup>a</sup> 70.80 <sup>b</sup>	99.4
3	toluene	1.4926 <sup>a</sup> 1.4940 <sup>b</sup>	110.7 <sup>a</sup> 110.63 <sup>b</sup>	99.6

<sup>a</sup> Measured. <sup>b</sup> Reference 15. <sup>c</sup> Reference 16.

Physics Model SP 4290 electronic integrator. The column was 3 m long and 0.2 cm in diameter. Column packing, operating temperature, and injector and detector temperatures were as follows: 20% O.V. 17, 120 °C, 210 °C, 220 °C for the binary system; GP 20% SP-2100/0.1% Carbowax 1500 on 100/120 Supelcoport, 100 °C, 230 °C, 230 °C, for the ternary system. Very good separation was achieved under these conditions, and calibration analyses were carried out to convert the peak ratio to the weight composition of the sample. Concentration measurements were accurate to better than ±1%. The accuracy in determination of pressure and temperature was  $\Delta P = \pm 1$  mmHg and  $\Delta t = \pm 0.02$  °C.

#### Results

The temperature-concentration measurements at 760 mmHg for the binary and ternary systems are reported in Figures 1 and